

EE200 DIGITAL LOGIC CIRCUIT DESIGN

Class Notes CLASS 2-2

The material covered in this class will be as follows:

- Complements
- Subtraction using complements.

By the end of this class you should be able to:

- Obtain the r 's and $(r-1)$'s complements in decimal, binary, and any other number system
- Perform subtraction by addition of the complements

Decimal number complements:

$$\begin{aligned} 9\text{'s complement of the decimal number } N &= (10^n - 1) - N \\ &= n \text{ (9's)} - N \end{aligned}$$

i.e. {subtract each digit from 9}

Example → 9's complement of 134795 is 865204

Similarly

$$1\text{'s complement of the binary number } N = (2^n - 1) - N = n \text{ (1's)} - N$$

Example → 1's complement of 110100101 is 001011010
which can be obtained by replacing each one by a zero and each zero by one.

r 's complement:

10's complement of the decimal number $N = 10^n - N = (r-1)$'s complement + 1

Example → 10's complement of 134795 is 865205

Example → find the 9's and 10's complements of 314700.

Answer → 9's complement = 685299
10's complement = 685300

Rule: To find the 10's complement of a decimal number leave all leading zeros unchanged. Then subtract the first non-zero digit from 10 and all the remaining digits from 9's.

The 2's complement of a binary number is defined in a similar way.

Example: Find the 1's and 2's complements of the binary number 1101001101

Answer → 1's complement is 0010110010
2's complement is 0010110011

Example: Find the 1's and 2's complements of 100010100

Answer → 1's complement is 011101011
2's complement is 011101100

Subtraction using r's complement:

To find $M-N$ in base r , we add $M + r$'s complement of N

Result is $M + (r^n - N)$

1) If $M > N$ then result is $M - N + rn$ (rn is an end carry and can be neglected).

2) If $M < N$ then result is $r^n - (N-M)$ which is the r 's complement of the result.

Example: Subtract $(76425 - 28321)$ using 10's complements.

Answer \rightarrow 10's complement of 28321 is 71679

$$\begin{array}{r} \text{Then add } \rightarrow \quad 76425 \\ \quad \quad \quad \quad + 71679 \\ \hline \text{Discard } \rightarrow \quad 148104 \end{array}$$

Therefore the difference is 48104 after discarding the end carry.

Example: subtract $(28531 - 345920)$

Answer \rightarrow It is obvious that the difference is negative. We also have to work with the same number of digits, when dealing with complements.

10's complement of 345920 is 654080

$$\begin{array}{r} \text{Then add } \rightarrow \quad 028531 \\ \quad \quad \quad \quad + 654080 \\ \hline \text{No end carry } \rightarrow \quad 682611 \end{array}$$

Therefore the difference is negative and is equal to the 10's complement of the answer.

Difference is $\rightarrow -317389$

The same rules apply to binary.

Example: subtract $(11010011 - 10001100)$

Answer → 2's complement of 10001100 is 01110100

Then add →

$$\begin{array}{r} 11010011 \\ + 01110100 \\ \hline 101000111 \end{array}$$

Discard

The difference is positive and is equal to 01000111

The same rules apply to subtraction using the (r-1)'s complements. The only difference is that when an end carry is generated, it is not discarded but added to the least significant digit of the result. Also, if no end carry is generated, then the answer is negative and in the (r-1)'s complement form.

Example: Subtract (76425 - 28321) using 9's complements.

Answer → 9's complement of 28321 is 71678

Then add →

$$\begin{array}{r} 76425 \\ + 71678 \\ \hline 148103 \\ \xrightarrow{\quad} 1 \\ \hline 48104 \end{array}$$

Difference

Example: subtract (11010011 - 10001100) using 1's complement.

Answer → 1's complement of 10001100 is 01110011

Then add →

$$\begin{array}{r} 11010011 \\ + 01110011 \\ \hline 101000110 \\ \xrightarrow{\quad} 1 \\ \hline \end{array}$$

Difference

101000111